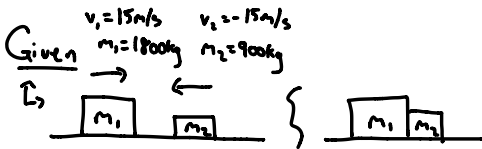


Momentum $+200 \quad -200$

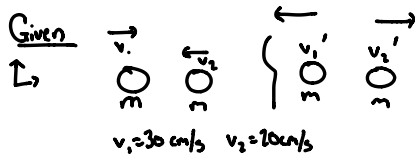
Energy $E_i \neq E_f$
 $\frac{1}{2}m_A v_A^2 + \frac{1}{2}m_B v_B^2 = 0$
 $200 + 400 = 0$
 $600 \neq 0$
 $\Delta KE = 0 - 600 = -600 \text{ J}$



Find a) v_f b) ΔKE

Solve a) $m_1 v_1 + m_2 v_2 = (m_1 + m_2) v_f$
 $v_f = \frac{(1800)(15) + (900)(-15)}{(1800 + 900)}$
 $v_f = \boxed{5.0 \text{ m/s}}$

b) $KE_i = \frac{1}{2}m_1 v_1^2 + \frac{1}{2}m_2 v_2^2$ $KE_f = \frac{1}{2}v_f^2 (m_1 + m_2)$
 $= (900)(15)^2 + (900)(15)^2 = \frac{1}{2}(5)^2 (2700)$
 $= 303750 \text{ J}$ $= 33750 \text{ J}$
 $\Delta KE = 33750 - 303750 = \boxed{-270000 \text{ J}}$



Find a) v_1', v_2'

Solve a) $m_1 v_1 + m_2 v_2 = m_1 v_1' + m_2 v_2'$
 $30 + (-20) = v_1' + v_2'$
 $10 = v_1' + v_2'$

$v_1 - v_2 = -(v_1' - v_2')$
 $30 - (-20) = v_2' - v_1'$
 $50 = v_2' - v_1'$

$60 = 2v_2'$
 $v_2' = \boxed{30 \text{ m/s}}$

$50 = (30) - v_1'$
 $v_1' = \boxed{-20 \text{ m/s}}$

Collision

Inelastic - Momentum conservation
 (Energy not cons.)
 - perfectly inelastic (stick together)

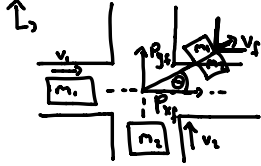
Elastic - Momentum cons.
 (K. Energy cons.)



Elastic

- ① $m_1 v_1 + m_2 v_2 = m_1 v_1' + m_2 v_2'$
- ② $\frac{1}{2}m_1 v_1^2 + \frac{1}{2}m_2 v_2^2 = \frac{1}{2}m_1 v_1'^2 + \frac{1}{2}m_2 v_2'^2$
- ③ $v_1 - v_2 = -(v_1' - v_2')$ Relative Velocity Equation

Given $m_1 = 1500 \text{ kg}$, $m_2 = 2500 \text{ kg}$
 $v_1 = 25 \text{ m/s}$, $v_2 = 20 \text{ m/s}$



Solve a) $m_1 v_1 = (m_1 + m_2) \cos \theta v_f$

$$\frac{m_1 v_1}{\cos \theta} = \frac{m_2 v_2}{\sin \theta}$$

$\perp p_{yi}$
 $m_2 v_2 = (m_1 + m_2) v_f \sin \theta$

$$\tan \theta = \frac{m_2 v_2}{m_1 v_1}$$

$$\theta = \tan^{-1} \left(\frac{2500 \cdot 20}{1500 \cdot 25} \right)$$

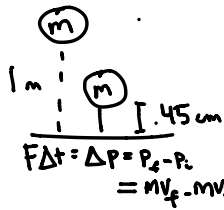
$$\theta = 53.1^\circ$$

$$v_f = \frac{m_1 v_1}{(m_1 + m_2) \cos \theta}$$

$$= \frac{1500 \cdot 25}{(4000) \cos(53.1)}$$

$$v_f = 15.6 \text{ m/s}$$

Find a) v_f, θ



$$V = \sqrt{2gh}$$

$$V_i = \sqrt{2(9.8)(1)}$$

$$V_f = \sqrt{2(9.8)(.45)}$$

$$F \Delta t = \Delta p = p_f - p_i$$

$$= m v_f - m v_i$$